

# Preparation and Characterization of Rare Earth Rhenium Oxides $Ln_6ReO_{12}$ , $Ln = Ho, Er, Tm, Yb, Lu$

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Compounds of the series  $Ln_6ReO_{12}$ ,  $Ln = Ho, Er, Tm, Yb, Lu$ , have been prepared by subsolidus reaction and are isotypic with  $Ln_6MoO_{12}$ ,  $Ln_6WO_{12}$ , and  $Ln_6UO_{12}$ , crystallizing in space group  $R\bar{3}$  with  $Z=3$  for the R-centered setting. The magnetic moment per rhenium ion in  $Lu_6ReO_{12}$  is  $0.74(1)\mu_B$ , and  $Yb_6ReO_{12}$  orders antiferromagnetically below  $2.15(10)$  K.

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**Key Words:** crystal structure; magnetic susceptibilities; rhenium (+VI) compounds.

## INTRODUCTION

Mixed oxides of composition  $MeO_3 \cdot Ln_2O_3$ , with  $Ln$  a rare earth element or yttrium, are known for the hexavalent metals  $Me = Mo, W, U$  (1). They crystallize in a rhombohedral structure related to the ordered  $Ln_7O_{12}$  phases. Furthermore, the stability ranges of this structure type in the ternary phase systems  $MeO_2$ – $MeO_3$ – $Ln_2O_3$  have been discussed, revealing a significant dependence on the specific cations (2). Accordingly, the formation of this structure type requires a minimum cation size ratio  $Me/Ln$  of 0.67. Based on this empirical criterion the same crystal structure was predicted for all the fictitious compounds  $Ln_6ReO_{12}$ , but the assumed ionic radius for  $Re^{6+}$  has not been reported. Only the existence of  $ReO_3 \cdot 3Y_2O_3$  is mentioned in the literature (3).

In this contribution we report on the synthesis of  $Ln_6ReO_{12}$  compounds with  $Ln = Ho, Er, Tm, Yb, Lu$ , which is essentially different from the preparation of the  $Mo, W, U$  compounds due to the high volatility of  $Re_2O_7$  and the multivalence of rhenium. In addition to the structures determined from X-ray powder data the magnetic properties of these compounds will be reported.

## EXPERIMENTAL

All compounds have been synthesized by subsolidus reaction. For this purpose the sesquioxides  $Ln_2O_3$  have been

mixed with  $ReO_2$  in the ratio 2:1, i.e., a ratio  $Ln:Re = 4:1$ . The reactants were intimately ground in an agate mortar under acetone and filled in a Pt/Rh(90/10%) tube under argon atmosphere. The tubes were welded to ensure that they were properly closed. The furnace was flushed with argon before heating the samples to  $1200^\circ C$  at a rate of  $300^\circ/h$ , tempering for 12 h, cooling to room temperature at a rate of  $180^\circ/h$  and afterward tempering again at  $1200^\circ C$  for 24 h at the same rates. A green-blackish powder was obtained which showed two distinct phases under a light microscope. Both kinds of specimen have further been investigated by X-ray powder diffraction, using a STOE STADI P diffractometer with germanium-monochromatized  $Cu K\alpha_1$  radiation and a position-sensitive detector with  $6^\circ$  aperture in transmission mode. The temperature dependence of magnetization at field strength of  $0.01 T$  for  $Ln = Ho, Er, Tm, Yb$  and  $0.25 T$  for  $Lu$  was measured down to 1.8 K with a superconducting quantum interference device (SQUID) from Quantum Design.

## RESULTS AND DISCUSSION

### Crystal Structure

All compounds  $Ln_6ReO_{12}$ ,  $Ln = Ho, \dots, Lu$ , gave very similar diffraction patterns, which could be indexed on the basis of a trigonal cell. The structure solution from powder data revealed the space group  $R\bar{3}$  with  $Z=3$  for the R-centered setting. The structural parameters have been refined by the Rietveld method using FULLPROF (5), resulting in the lattice constants listed in Table 1. Atomic parameters in Table 2 and the corresponding observed and calculated profiles together with the difference curve in Fig. 1 are given for  $Tm_6ReO_{12}$  as a representative. Isotropic temperature factors have been applied for the oxygen atoms, but anisotropic ones for the  $Ln$  and  $Re$  atoms, for the latter restricted by local site symmetry to only two independent parameters. In the case of  $Ln = Lu$  the  $Lu:Re$  ratio was confirmed to be  $6.0(1)$  by EDX.  $[ReO_6]$ -octahedra are connected with 12  $[LnO_7]$ -units by common oxygens, to six of

**TABLE 1**  
Cell Parameters for the Compounds  $Ln_6ReO_{12}$  as Determined from Powder X-Ray Diffraction Data by Rietveld Refinement

$Ln$	$a$ (Å)	$c$ (Å)
Ho	9.7621 (3)	9.3016 (3)
Er	9.7291 (2)	9.2553 (2)
Tm	9.6953 (3)	9.2084 (3)
Yb	9.6425 (3)	9.1672 (3)
Lu	9.6269 (2)	9.1316 (2)

Note. The sigmas are in agreement with (4).

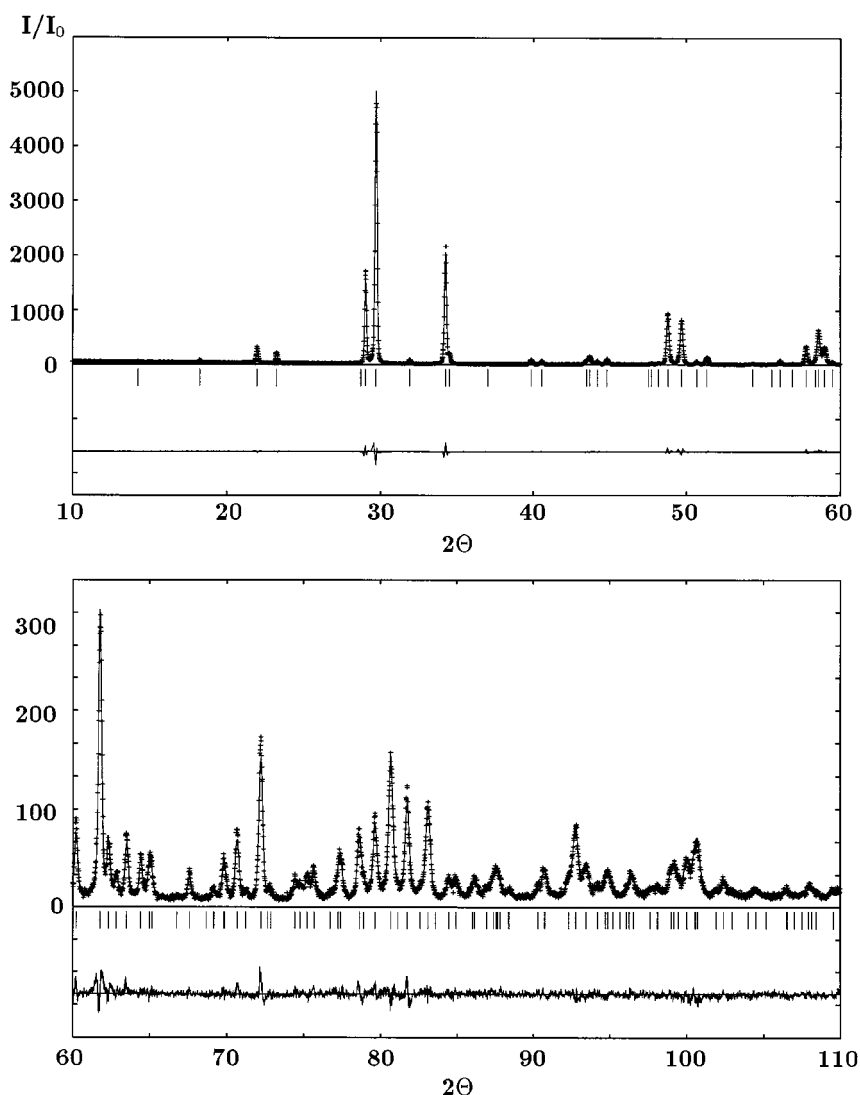
them by sharing edges and to six others by sharing corners. The crystal structure is shown in Fig. 2. The second phase in the reaction mixture was identified to be  $Ln_3ReO_8$  with fluorite-type structure (6).

**TABLE 2**  
Atomic Parameters for  $Tm_6ReO_{12}$  as Representatives for the Series of Isotypic Compounds  $Ln_6ReO_{12}$ ,  $Ln = Ho, \dots, Lu$

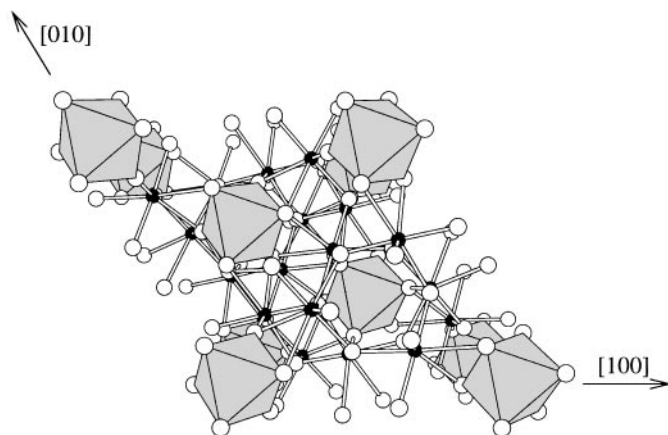
Atom	Site	$x$	$y$	$z$	$B_{\text{eff}}$
Re	$3a$	0	0	0	0.47(7)
Tm	$18f$	0.2527(3)	0.0411(5)	0.3543(3)	0.55(2)
O1	$18f$	0.185(3)	0.042(4)	0.113(2)	1.3(6)
O2	$18f$	0.226(3)	0.031(4)	0.599(2)	1.2(5)

Note. The uncertainties are calculated in agreement with (4). Only isotropic temperature factors have been refined for the oxygen atoms, while one third of the trace of the anisotropic tensor is given for the Tm and Re atoms.

The compounds  $Ln_6ReO_{12}$ ,  $Ln = Ho, \dots, Lu$ , are the first examples of rare earth rhenium oxides with a formal oxidation state of rhenium + VI. This series offers a suitable test



**FIG. 1.** The observed and fitted profiles for  $Tm_6ReO_{12}$  and the corresponding difference curve ( $CuK\alpha_1$ ). The powder pattern has been split into two parts with different scales for clarity.



**FIG. 2.** The crystal structure of  $Ln_6ReO_{12}$ , view along the  $[001]$  direction.  $[ReO_6]$  octahedra and  $Ln-O$  bonds are shown for all cations in one unit cell, including all Re ions on the corners. Some oxygen atoms outside the unit cell are also shown to complete the coordination polyhedra for all Re and  $Ln$  ions.

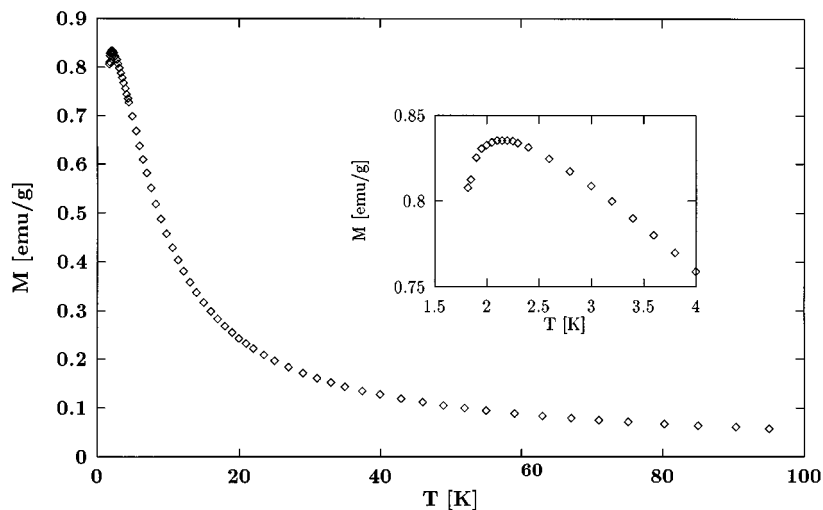
for the empirical stability criterion for this structure type, previously deduced for the Mo, W, and U series (2). Accordingly, this rhombohedral structure type should only be formed if the ratio between the ionic radii of the hexavalent metal ions and the trivalent rare-earth ion is at least 0.67. Using a consistent set of ionic radii for sixfold coordination of the metal ions (7), slightly different ratios are obtained. The relevant values are summarized in Table 4. Although the  $Re^{6+}$  ion is much smaller than  $W^{6+}$  and  $Mo^{6+}$ , the stability edge of  $Ln_6ReO_{12}$  is not shifted to smaller rare earth elements, but just in between those of W and Mo. The largest rare earth element forming the  $Ln_6MeO_{12}$  structure

**TABLE 3**  
**Magnetic Properties of the Compounds  $Ln_6ReO_{12}$**

$Ln$	$\mu(Ln^{3+})/\mu_B$	$\Theta/K$	$M_0/(\text{emu/g})$	$T$ range
Ho	8.91(4)	-0.21	$1.2 \cdot 10^{-4}$	10-180 K
Er	9.25(8)	-11.5	$4.2 \cdot 10^{-6}$	25-180 K
Tm	7.15(6)	-12.7	$9.6 \cdot 10^{-7}$	20-50 K
Yb	3.19(3)	-2.03	$1.8 \cdot 10^{-5}$	10-100 K
Lu	—	-1.29	$2.4 \cdot 10^{-4}$	1.8-80 K

*Note.* The same magnetic moment per  $Re^{6+}$  ion of  $0.74\mu_B$  was assumed for all compounds as deduced from the temperature dependence of magnetization in  $Lu_6ReO_{12}$  with only diamagnetic rare earth ions. Only data within the given temperature range have been used to determine the Curie-Weiss parameters.

type is Er for  $Me = Mo$ , Dy for  $Me = W$ , and Ho for  $Me = Re$ . The  $U^{6+}$  ion is sufficiently large to build up this structure type for all rare earth elements and for yttrium. The stability limit can be given by a common critical ratio  $Me/Ln$  of 0.655 for  $Me = Mo, W, \text{ or } U$ , but a value of 0.605 is deduced for the case of  $Me = Re$ . Nevertheless, it is confirmed that the stability range is limited by a critical size of the rare earth ion, even if this critical size cannot be related to the size of the hexavalent ion as proposed. In particular for the case of rhenium, which occurs in the formal oxidation states +4, +5, +6, and +7 with calculated ionic radii varying from 0.63 to 0.53 Å for sixfold coordination, it is questionable which value should be applied to the above mentioned stability criterion. As we start with rheniumdioxide, i.e.,  $Re^{+4}$  and end up with  $Re^{+6}$ , an intermediate ionic radius of 0.605 Å can fit the analogy to the Mo, W, and U series.



**FIG. 3.** Temperature dependence of magnetization for  $Yb_6ReO_{12}$ . The low temperature behavior is exposed in the inset.

**TABLE 4**  
**Ionic Radii in Å of Selected Ions in Sixfold Coordination as Taken from (7) and Ratios, Relevant for the Stability Criterion**

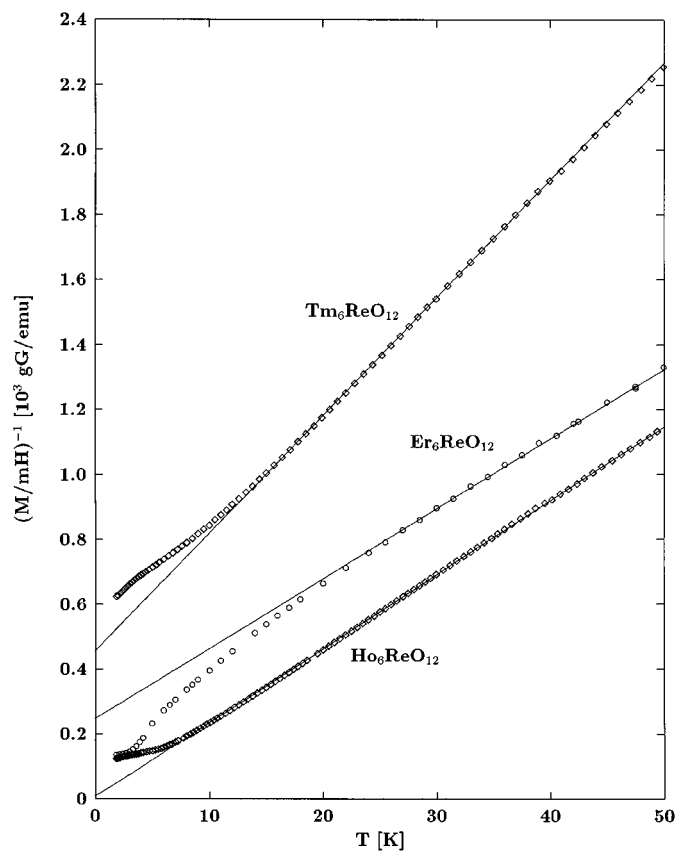
$\text{Mo}^{+6}$	0.59	$\text{Y}^{3+}$	0.900	$\text{Dy}^{3+}$	0.912
$\text{W}^{+6}$	0.60	$\text{La}^{3+}$	1.032	$\text{Ho}^{3+}$	0.901
$\text{Re}^{+6}$	0.55	$\text{Gd}^{3+}$	0.938	$\text{Er}^{3+}$	0.890
$\text{U}^{+6}$	0.73	$\text{Tb}^{3+}$	0.923	$\text{Lu}^{3+}$	0.861
Mo:Y	0.656	W:Y	0.667	Re:Y	0.611
Mo:Ho	0.655	W:Gd	0.640	Re:Dy	0.603
Mo:Er	0.663	W:Dy	0.658	Re:Ho	0.610

### Magnetic Properties

The observed temperature dependences of magnetization have been fitted by a Curie-Weiss law, modified by an additional temperature independent contribution  $M_0$ ,

$$M(T) = \frac{C}{T - \Theta} + M_0. \quad [1]$$

A magnetic moment of  $0.74(1) \mu_B$  per  $\text{Re}^{6+}$  ion was deduced from the Curie constant for  $Ln = \text{Lu}$ . The magnetic moments for the rare earth elements are given in Table 3, based on the same rhenium contribution in all compounds.  $\text{Re}^{+6}$  is one of the very rare examples of a  $5d^1$  electron configuration. In a crystal field of octahedral symmetry the five  $L = 2$  states split into a low-lying triplet and a doublet. In the limiting case of infinite crystal field splitting and ideal cubic symmetry, the ground state with effective angular momentum  $\tilde{J} = 3/2$  has the Landé factor  $g(\tilde{J}) = 0$ . The observed magnetic moment of  $\text{Re}^{+6}$  has an anisotropic contribution from further splittings of the triplet due to crystal field effects of lower symmetry and an isotropic contribution due to the finite splitting between doublet and triplet. Both effects can be distinguished based on the anisotropy of the  $g$ -tensor, but the experimental determination of its matrix elements requires a single crystal of sufficient size for paramagnetic resonance spectroscopy, which could not be prepared so far. Down to 1.85 K antiferromagnetic ordering is only suggested for  $Ln = \text{Yb}$  from the pronounced maximum of magnetization at  $T = 2.15(10)$  K; see Fig. 3. Nevertheless, deviations from the Curie-Weiss law are also observed at low temperatures for  $Ln = \text{Ho}$ ,  $\text{Er}$ , and  $\text{Tm}$  as shown for the inverse magnetization in Fig. 4.



**FIG. 4.** Temperature dependence of the inverse magnetization for  $\text{Ho}_6\text{ReO}_{12}$ ,  $\text{Er}_6\text{ReO}_{12}$ , and  $\text{Tm}_6\text{ReO}_{12}$ . The drawn lines belong to modified Curie-Weiss fits with the parameters of Table 3.

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